



**NTNU – Trondheim**  
Norwegian University of  
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# Introduction to the Unit Commitment Problem in Electric Power Production

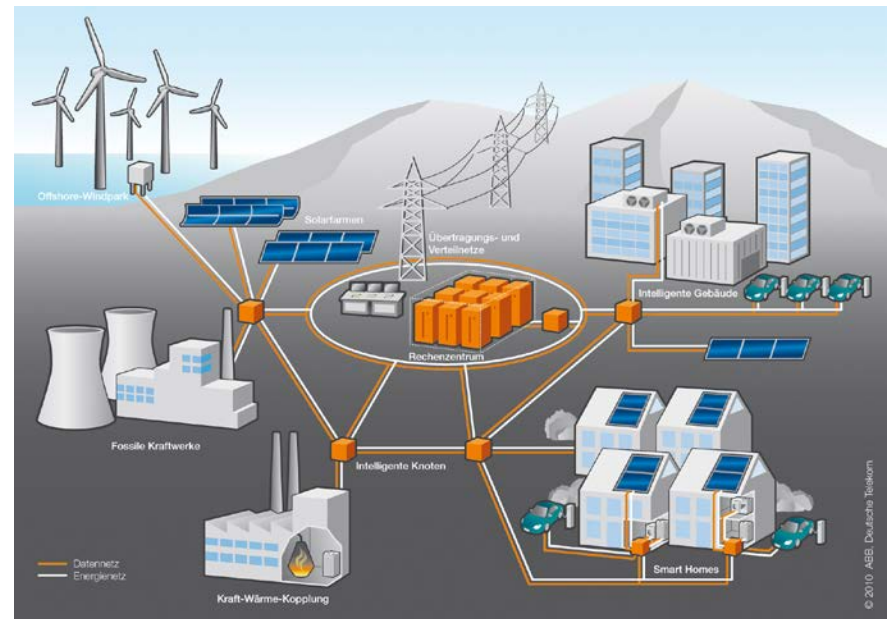
# Outline

1. Problem definition.
2. The structure of electric power generation
  1. Norway.
  2. The US.
3. The unit commitment and economic dispatch problem.
  - Various extension.
4. Solution approaches.

# Unit commitment (UC)

## Basic definition:

To find the **least cost** dispatch of available generation resources to meet an **estimated electric power demand** over a given time horizon.



Source: abb.de

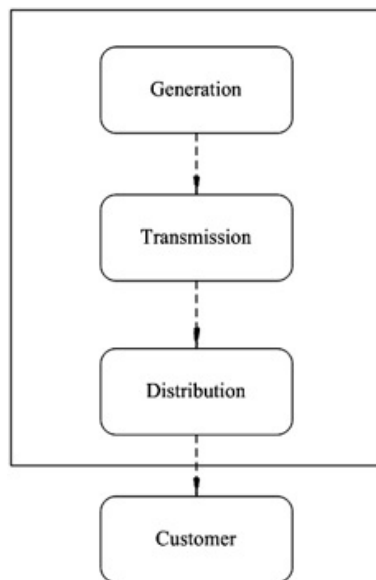
A variety of versions:

- Level of integration.
- Constraints included such as emission or security-of-supply constraints.
- Time horizon.
- Cost minimization or profit maximization.

# Electricity market:

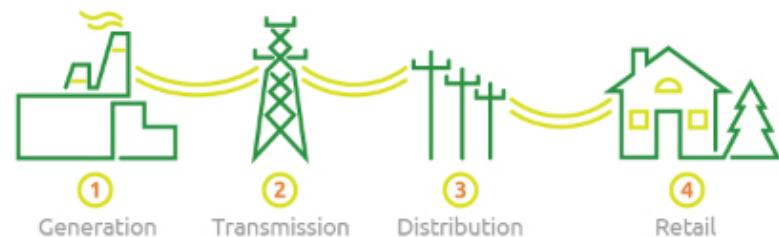
## Regulated markets

- **One** utility controlling the power production for a whole region.
- Minimizing cost = maximizing profit.
- Vertical integration (monopoly)



## Deregulated markets

- **Several utilities** competing of being the most attractive provider of electricity.
- Different providers for different services.
- Generating companies (GENCOs) try to maximize their profit: revenue from sales minus generation cost.
- Independent system operators (**ISO**) coordinate, control and monitor the operations of the electrical power systems.



Source: xenogyre.com/

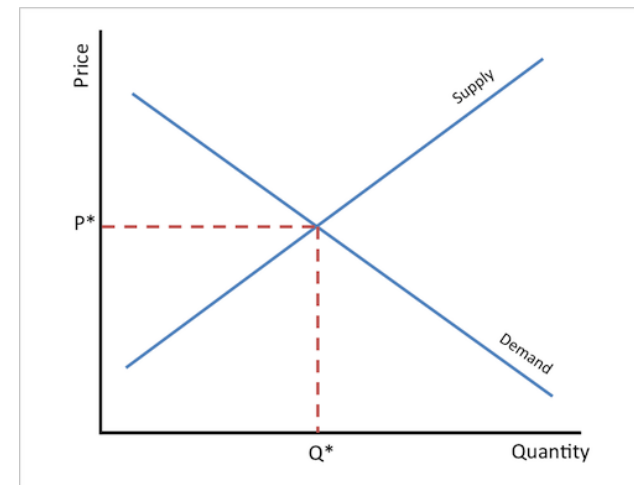
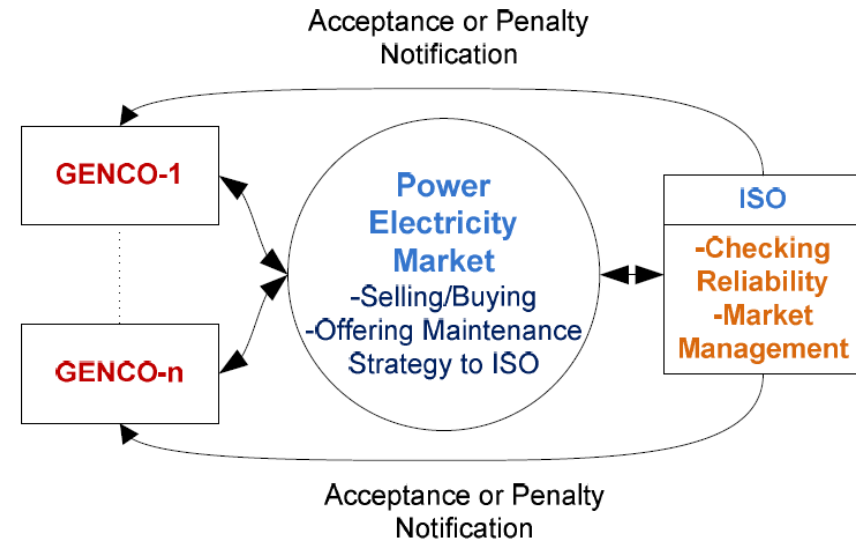
# UC - a bid and auction system

Source: Manbachi et al

Basic sequence of trading for day-ahead UC

1. Transmission companies delivers capacity estimates in an area.
2. Power suppliers (sellers) delivers their offers → **supply curve**.
3. Buyers give bid on how much power there are willing to buy at which price → **demand curve**.
4. ISO adjust curves to ensure sufficient supply and a partly control prices to prevent squeezing of small suppliers and to maintain on acceptable prices for customers.
5. Prices is cleared – prices are set.

Note: Many variants in integration of ISOs and GENCOs



Market clearing price

# Adjusting the UC schedule

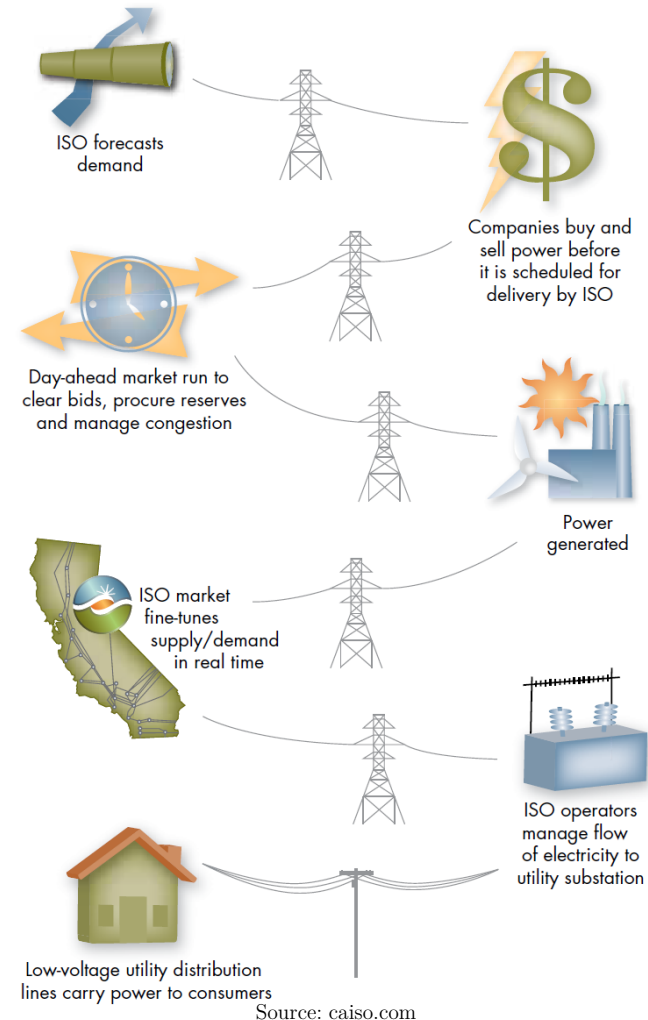
Power levels and units committed must be

## adjustment:

- Consumption differs from forecasted demand.
- Intermittent, stochastic resources (wind mills, solar cells etc.)

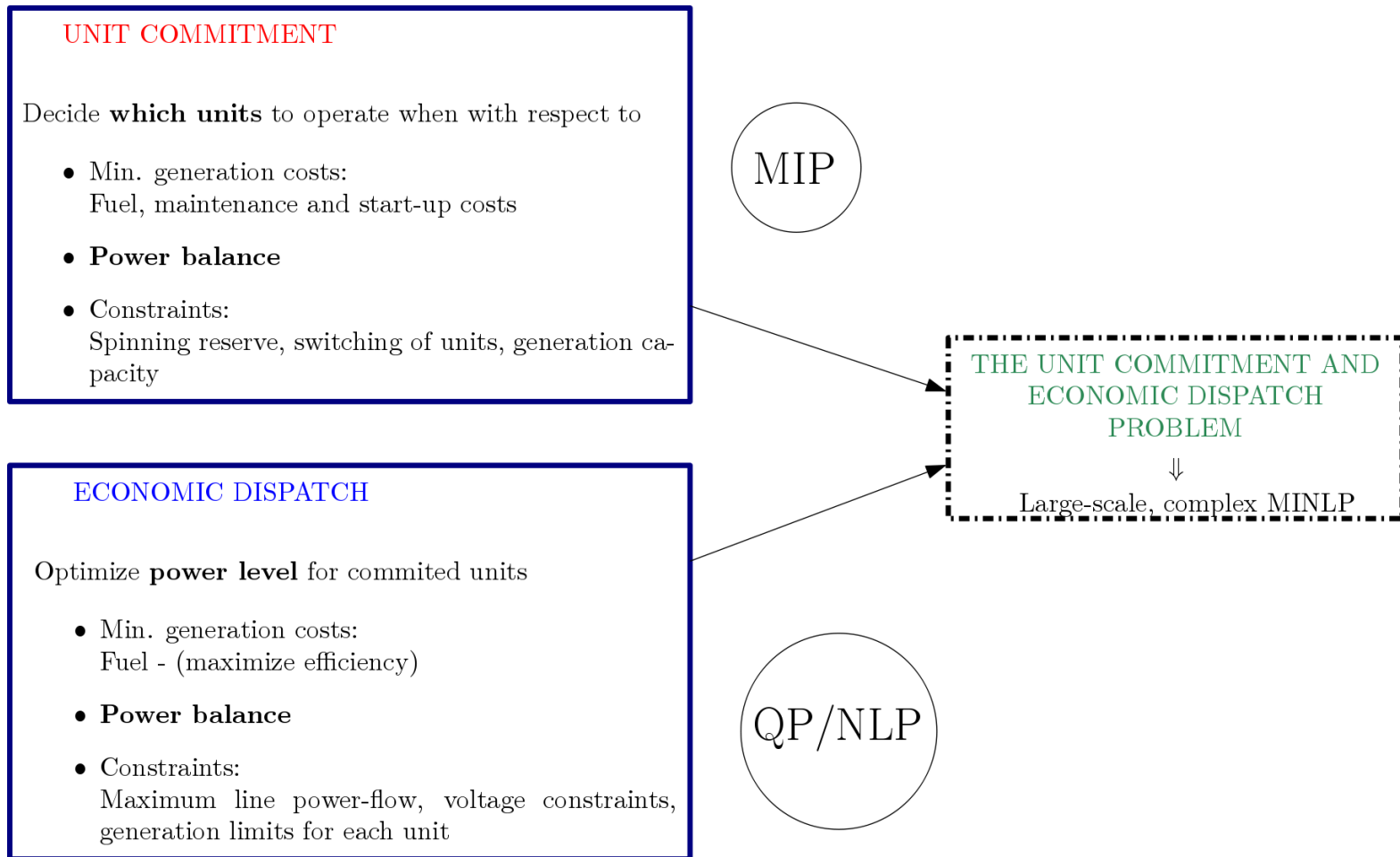
Different markets with different horizons:

1. Day ahead market: 24 hours – hourly dispatch plans.
2. Look-ahead unit commitment
  - Constantly adjust status of fast-starting units to ensure reliability of supply and meet *system changes* within the next 3-6 hours.
3. Real-time market:
  - Recommit very fast units (water, natural-gas) based on actual system operating conditions.
  - Time frame: 15 minutes to 2 hours.



# Unit commitment and economic dispatch

Given a forecasted demand  $d_k$  from an independent system operator (ISO)



# The conventional **unit commitment** problem

- Objective function: minimize total costs.
- Constraints shared by all units (global constraints):
  - Power demand.
  - Spinning reserve.
- Constraints for each unit:
  - Power capacity (min/max).
  - Minimum up down-time constraints.
  - Ramping constraints.



# Extension of the unit commitment problem 1:

## Emission-constrained unit commitment

1. Hard upper bound (constraints) on allowed emissions.
2. Penalty/cost on emissions in the objective function.
3. Emission allowance system (cap and trade).



Source: pennenergy.com

# Extension of the unit commitment problem 2:

## Stochastic unit commitment:

1. Uncertainty in demand.
2. Intermittent renewable generation resources.
3. Capacity of generators
  - Generators dropping out.
4. Varying fuel prices.



# Extension of the unit commitment problem 3:

## Security-constrained unit commitment

- Sufficient spinning reserves:
  - Abrupt changes in load.
  - Units dropping out.
- Transmission capacity.
- Natural-gas availability.



Source: <http://buildipedia.com/>



Source: [forbes.com](http://forbes.com)

# Solution approaches for UC

- Solve as large-scale MILP or MINLP – need a tight formulation.
- Units are coupled by power balance and spinning reserve: Utilize block structure and apply a decomposition approach:
  - Lagrangian relaxation/decomposition

